

WORKSHEET:SOLUTIONS AND COLLIGATIVE PROPERTIES  
Chem 111

**SET A:**

- 1) Find the molarity of all ions in a solution that contains 0.165 moles of aluminum chloride in 820. ml solution.



Answer:  $[\text{Al}^{3+}] = 0.201 \text{ M}$ ,  $[\text{Cl}^-] = 0.603 \text{ M}$ .

$$[\text{Al}^{3+}] = \frac{0.165 \text{ mole AlCl}_3}{0.820 \text{ L}} \left( \frac{1 \text{ mole Al}^{3+}}{1 \text{ mole AlCl}_3} \right) = 0.201 \quad \frac{\text{mole Al}^{3+}}{\text{L}}$$

$$[\text{Cl}^-] = \frac{0.165 \text{ mole AlCl}_3}{0.820 \text{ L}} \left( \frac{3 \text{ moles Cl}^-}{1 \text{ mole AlCl}_3} \right) = 0.603 \quad \frac{\text{moles Cl}^-}{\text{L}}$$

- 2) Find the molarity of each ion present after mixing 27 ml of 0.25 M  $\text{HNO}_3$  with 36 ml of 0.42 M  $\text{Ca}(\text{NO}_3)_2$ .  
(Note: There is no reaction taking place.)

Answer:  $[\text{H}^+] = 0.11 \text{ M}$ ,  $[\text{NO}_3^-] = 0.58 \text{ M}$ ,  $[\text{Ca}^{2+}] = 0.24 \text{ M}$ .

$$1) \text{Find moles HNO}_3: \quad M_{\text{HNO}_3} V_{\text{HNO}_3} = 0.25 \frac{\text{mole}}{\text{L}} \times 0.027 \text{ L} = 6.8 \times 10^{-3} \text{ mole}$$

$$2) \text{Find moles Ca}(\text{NO}_3)_2: \quad M_{\text{Ca}(\text{NO}_3)_2} V_{\text{Ca}(\text{NO}_3)_2} = 0.42 \frac{\text{mole}}{\text{L}} \times 0.036 \text{ L} = 1.5 \times 10^{-2} \text{ mole}$$

$$[\text{H}^+] = \frac{6.8 \times 10^{-3} \text{ mole H}^+}{0.063 \text{ L}} = 0.11 \text{ M}$$

$$[\text{Ca}^{2+}] = \frac{1.5 \times 10^{-2} \text{ mole Ca}(\text{NO}_3)_2}{0.063 \text{ L}} \left( \frac{1 \text{ mole Ca}^{2+}}{1 \text{ mole Ca}(\text{NO}_3)_2} \right) = 0.24 \text{ M}$$

\* moles  $\text{NO}_3^-$  from  $\text{HNO}_3$ :

$$6.8 \times 10^{-3} \text{ mole HNO}_3 \left( \frac{1 \text{ mole } \text{NO}_3^-}{1 \text{ mole HNO}_3} \right) = 6.8 \times 10^{-3} \text{ mole } \text{NO}_3^-$$

\* moles  $\text{NO}_3^-$  from  $\text{Ca}(\text{NO}_3)_2$ :

$$1.5 \times 10^{-2} \text{ mole Ca}(\text{NO}_3)_2 \left( \frac{2 \text{ moles } \text{NO}_3^-}{1 \text{ mole Ca}(\text{NO}_3)_2} \right) = 3.0 \times 10^{-2} \text{ mole } \text{NO}_3^-$$

$$[\text{NO}_3^-] = \frac{(6.8 \times 10^{-3} + 3.0 \times 10^{-2}) \text{ mole } \text{NO}_3^-}{0.063 \text{ L}} = 0.58 \text{ M}$$

3) Find the molarity of each ion present after mixing 35 ml of 0.42 M  $K_2SO_4$  with 27 ml of 0.17 M  $K_3PO_4$ .  
 Answer:  $[K^+] = 0.71\text{M}$ ,  $[SO_4^{2-}] = 0.24\text{ M}$ ,  $[PO_4^{3-}] = 0.074\text{ M}$ .

Find moles  $K_2SO_4$ :

$$M_{K_2SO_4} V_{K_2SO_4} = 0.42 \frac{\text{mole}}{\text{l}} \times 0.035\text{l} = 0.015 \text{ mole } K_2SO_4$$

Find moles of  $K_3PO_4$ :

$$M_{K_3PO_4} V_{K_3PO_4} = 0.17 \frac{\text{mole}}{\text{l}} \times 0.027\text{l} = 4.6 \times 10^{-3} \text{ mole } K_3PO_4$$

Find conc. of  $SO_4^{2-}$ :

$$0.015 \text{ mole } K_2SO_4 \left( \frac{1 \text{ mole } SO_4^{2-}}{1 \text{ mole } K_2SO_4} \right) = 0.015 \text{ mole } SO_4^{2-}$$

$$[SO_4^{2-}] = \frac{0.015 \text{ mole}}{0.062\text{l}} = 0.24 \text{ M}$$

Find conc. of  $K^+$ :

$$0.015 \text{ mole } K_2SO_4 \left( \frac{2 \text{ mole } K^+}{1 \text{ mole } K_2SO_4} \right) = 0.030 \text{ mole } K^+$$

$$4.6 \times 10^{-3} \text{ mole } K_3PO_4 \left( \frac{3 \text{ moles } K^+}{1 \text{ mole } K_3PO_4} \right) = 0.014 \text{ mole } K^+$$

$$[K^+] = \frac{(0.030 + 0.014) \text{ mole } K^+}{0.062\text{l}} = 0.71 \text{ M}$$

Find conc. of  $PO_4^{3-}$ :

$$[PO_4^{3-}] = \frac{0.0046 \text{ mole } PO_4^{3-}}{0.062\text{l}} = 0.074 \text{ M}$$

4) Calculate the concentration of each ion and the mass of any precipitate when a 0.300 mole of aluminum hydroxide is added to 50.0 ml of 2.5 M nitric acid solution (Assume that there is no volume change upon the addition of the aluminum hydroxide to the solution).

Hint: Write a balanced equation for the reaction taking place.

Answer: 20.0 g Al(OH)<sub>3</sub> left over, [Al<sup>3+</sup>] = 0.83M, [NO<sub>3</sub><sup>-</sup>] = 2.5 M



Find limiting reagent:

~~# moles HNO<sub>3</sub>~~ = M<sub>HNO<sub>3</sub></sub> V<sub>HNO<sub>3</sub></sub> = 2.5 mole L × .0500 L = ~~# moles HNO<sub>3</sub>~~ = 0.13 mole HNO<sub>3</sub>

Theoretical ratio of moles:  $\frac{\# \text{ moles HNO}_3}{\# \text{ moles Al(OH)}_3} = \frac{3}{1}$

Available ratio of moles:  $\frac{0.13 \text{ mole HNO}_3}{.300 \text{ mole Al(OH)}_3} = \frac{.43}{1}$

HNO<sub>3</sub> is the limiting reagent.

Find mass of Al(OH)<sub>3</sub> reacting

$$.12 \text{ mole HNO}_3 \left( \frac{1 \text{ mole Al(OH)}_3}{3 \text{ moles HNO}_3} \right) = .041 \text{ mole Al(OH)}_3 \text{ reacting}$$

Find mass of Al(OH)<sub>3</sub> left over:-

$$.300 \text{ mole Al(OH)}_3 \text{ available} - .042 \text{ mole Al(OH)}_3 \text{ reacting} \\ = 0.258 \text{ mole Al(OH)}_3 \text{ left over}$$

$$.258 \text{ mole Al(OH)}_3 \left( \frac{78.0 \text{ g Al(OH)}_3}{1 \text{ mole Al(OH)}_3} \right) = 20.2 \text{ g Al(OH)}_3 \text{ left over}$$

Find moles Al(NO<sub>3</sub>)<sub>3</sub> produced:

$$0.125 \text{ mole HNO}_3 \left( \frac{1 \text{ mole Al(NO}_3)_3}{3 \text{ moles HNO}_3} \right) = 0.0417 \text{ mole Al(NO}_3)_3$$

$$.0417 \text{ mole Al(NO}_3)_3 \left( \frac{1 \text{ mole Al}^{3+}}{1 \text{ mole Al(NO}_3)_3} \right) = .0417 \text{ mole Al}^{3+}$$

$$[\text{Al}^{3+}] = \frac{.0417 \text{ mole Al}^{3+}}{.0500 \text{ L}} = .83 \text{ M}$$

$$.0417 \text{ mole Al(NO}_3)_3 \left( \frac{3 \text{ moles NO}_3^-}{1 \text{ mole Al(NO}_3)_3} \right) = 0.125 \text{ mole NO}_3^-$$

$$[\text{NO}_3^-] = \frac{0.125 \text{ mole}}{.0500 \text{ L}} \neq 2.5$$

5) A solution consists of 3.88 g benzene,  $C_6H_6$ , and 2.45 g toluene,  $C_6H_5CH_3$ . The vapor pressure of pure benzene at  $20^\circ C$  is 75 mm Hg and that of toluene at  $20^\circ C$  is 22 mm Hg. Assume that Raoult's law holds for each component of the solution, calculate the mole fraction of benzene in the vapor. (molar mass of benzene = 78.0 g/mole and toluene = 92.0 g/mole.)

Answer: 0.87

$$\begin{aligned}
 \textcircled{1} \quad P_{\text{total}} &= P_{\text{benzene}} + P_{\text{toluene}} \\
 &= X_{\text{benzene}} P_{\text{benzene}}^{\circ} + X_{\text{toluene}} P_{\text{toluene}}^{\circ} \\
 &= \frac{3.88 \text{ g}}{78.0 \text{ g/mole}} (75 \text{ torr}) + \frac{2.45 \text{ g}}{92.0 \text{ g/mole}} (22 \text{ torr}) \\
 &= \frac{3.88}{78.0} + \frac{2.45}{92.0} \\
 &= \frac{.0497 \text{ mole}}{(.0497 + .0266) \text{ mole}} (75 \text{ torr}) + \frac{.0266 \text{ mole}}{.0266 + .0497 \text{ mole}} (22 \text{ torr}) \\
 &= .651 (75 \text{ torr}) + .349 (22 \text{ torr}) \\
 &= 49 \text{ torr} + 7.8 \text{ torr} \\
 &= 56.8 \text{ torr} = 57 \text{ torr}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{2} \quad X_{\text{benzene}} &= \frac{P_{\text{benzene}}}{P_{\text{total}}} \\
 &= \frac{49}{57 \text{ torr}} \\
 &\approx 0.86
 \end{aligned}$$

6) The freezing point of a glucose solution ( $C_6H_{12}O_6$ ; molar mass = 180.0 g/mole) is  $-10.3^\circ C$ . The density of the solution is 1.50 g/ml. What is the molality of the glucose solution? ( $K_f$  for water is  $1.86^\circ C \cdot \text{kg}/\text{mole}$ )

Answer: 4.16 mole/L

$$\textcircled{1} \quad \Delta T_{f.p} = K_{f.p} \text{ molality}$$

$$10.3^\circ C = 1.86 \frac{{}^\circ C \cdot \text{kg}}{\text{mole}} (\text{molality})$$

$$\text{molality} = \frac{10.3^\circ C}{1.86 \frac{{}^\circ C \cdot \text{kg}}{\text{mole}}} = 5.54 \frac{\text{mole}}{\text{kg}}$$

$$\textcircled{2} \quad \text{mass of solute} = 5.54 \text{ mole glucose} \left( \frac{180.0 \text{ g glucose}}{1 \text{ mole glucose}} \right) = 997 \text{ g glucose}$$

$$\textcircled{3} \quad \text{mass of solution} = 1000 \text{ g H}_2\text{O} + 997 \text{ g glucose} = 1997 \text{ g solution}$$

in 1000 g  $H_2O$   
containing 5.54 mole glucose

4) Volume of solution:

$$1997 \text{ g solution} \left( \frac{1 \text{ ml solution}}{1.50 \text{ g solution}} \right) = 1331 \text{ ml solution}$$

$$= 1.331 \text{ L solution}$$

containing 5.54 mole glucose

$$\textcircled{5} \quad \text{Molality} = \frac{5.54 \text{ mole glucose}}{1.331 \text{ L solution}} = 4.16 \text{ mole/L}$$

7) What is the normal boiling point of a 2.70 M solution of KBr that has a density of 1.80 g/ml? (K<sub>B</sub> for H<sub>2</sub>O is 0.512 °C .kg/mole)  
 Answer=: 101.9 °C

$$2.70 \text{ mole KBr} \left( \frac{119 \text{ g KBr}}{1 \text{ mole KBr}} \right) = 321 \text{ g KBr}$$

$\underbrace{\qquad\qquad\qquad}_{\text{in 1000 ml solution}}$

$$1000 \text{ ml solution} \left( \frac{1.80 \text{ g solution}}{1 \text{ ml solution}} \right) = 1800 \text{ g solution}$$

$$= 1.80 \times 10^3 \text{ g solution}$$

mass of H<sub>2</sub>O:

$$1800 \text{ g solution} - 321 \text{ g KBr} = 1479 \text{ g H}_2\text{O} = 1.479 \times 10^3 \text{ g H}_2\text{O}$$

$\underbrace{\qquad\qquad\qquad}_{\text{containing 2.70 mole KBr}}$

$$\text{molality} = \frac{2.70 \text{ mole KBr}}{1.479 \text{ kg H}_2\text{O}} = 1.83 \text{ mole/kg}$$

$$\Delta T_{B.P} = i \cdot K_{B.P} \text{ molality}$$

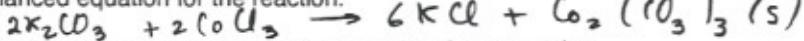
$$= 2 \frac{\text{particles}}{\text{formula units}} \cdot 0.512 \frac{\text{°C kg}}{\text{mole}} \times 1.83 \frac{\text{mole}}{\text{kg}}$$

$$= 1.87 \text{ °C}$$

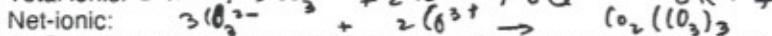
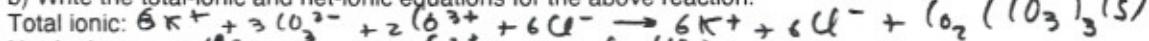
$$\text{normal B.P} = 100 + 1.87 = 101.9 \text{ °C}$$

g) 28.00 ml of 0.670 M potassium carbonate solution is mixed with 15.00 ml of 0.940 M cobalt(III) chloride

a) Write a balanced equation for the reaction.



b) Write the total-ionic and net-ionic equations for the above reaction.



c) Give the name and mass of any precipitate(s) that may have formed.

Answer: 1.87 g of  $Co_2(CO_3)_3$  precipitate.

Calculate the molar concentration of each ion remaining in solution after the reaction is complete.

Answer: concentration of potassium ions = 0.874 M,

concentration of cobalt (III) ions = 0.0372 M

concentration of carbonate ions = 0 M

concentration of chloride ions = 0.986 M

(c) Find limiting reagent:-

$$\text{no. of moles } K_2CO_3 = M_{K_2CO_3} V_{K_2CO_3} = 0.0280L \times 0.670 \frac{\text{mole}}{L} = 0.0188 \text{ mole}$$

$$\text{no. of moles } CoCl_3 = M_{CoCl_3} V_{CoCl_3} = 0.01500L \times 0.940 \frac{\text{mole}}{L} = 0.0141 \text{ mole available}$$

Theoretical ratio of moles:

$$\frac{\text{moles } K_2CO_3}{\text{moles } CoCl_3} = \frac{3}{1} ;$$

Available ratio of moles:

$$\frac{\text{moles } K_2CO_3}{\text{moles } CoCl_3} = \frac{0.0188 \text{ mole}}{0.0141 \text{ mole}} = \frac{1.33}{1}$$

Therefore,  $K_2CO_3$  is the limiting reagent

$$0.0188 \text{ mole } K_2CO_3 \left( \frac{1 \text{ mole } Co_2(CO_3)_3}{3 \text{ moles } K_2CO_3} \right) \left( \frac{297.89 \text{ g } Co_2(CO_3)_3}{1 \text{ mole } Co_2(CO_3)_3} \right) = 1.87 \text{ g of } Co_2(CO_3)_3 \text{ precipitate}$$

$$\text{d) moles of } CoCl_3 \text{ reacting: } 0.0188 \text{ mole } K_2CO_3 \left( \frac{2 \text{ moles } CoCl_3}{3 \text{ moles } K_2CO_3} \right) = 0.0125 \text{ moles } CoCl_3 \text{ reacting}$$

moles  $CoCl_3$  left over:

$$0.0141 \text{ mole } CoCl_3 \text{ available} - 0.0125 \text{ mole } CoCl_3 \text{ reacting} = 0.0016 \text{ mole } CoCl_3 \text{ left over}$$

$$0.0188 \text{ mole } K_2CO_3 \left( \frac{6 \text{ moles } KCl}{3 \text{ moles } K_2CO_3} \right) = 0.0376 \text{ mole } KCl \text{ forming}$$

$$[Co^{3+}] = \frac{0.0016 \text{ mole}}{0.0430 \text{ L}} = 0.0372 \text{ M}$$

$$[K^+] = \frac{0.0376 \text{ mole}}{0.0430 \text{ L}} = 0.874 \text{ M}$$

$$[Cl^-] = \frac{(0.0016 \times 3 + 0.0376) \text{ mole}}{0.0430 \text{ L}} = \frac{(0.0048 + 0.0376) \text{ mole}}{0.0430 \text{ L}}$$

$$= 0.986 \text{ M}$$

$$[CO_3^{2-}] = 0 \text{ M}$$

**SET B:**

1) A solution that contains 12.6 g of a nonvolatile nondissociating solute in 400. g of benzene freezes at 3.6 °C. The normal freezing point of benzene is 5.5 °C. What is the molar mass of the solute? (K<sub>f</sub> for benzene = 4.96 °C/kg/mole)

Answer: 82 g/mole

$$\textcircled{1} \quad \Delta T_f = K_f \text{ molality}$$

~~Two sig fig.~~  $1.9^\circ\text{C} = \left(4.96 \frac{\text{°C}}{\text{mole}} \cdot \text{kg}\right) \text{ molality}$   
~~Two sig fig.~~ molality =  $0.383 \frac{\text{mole}}{\text{kg}}$

$$\textcircled{2} \quad \text{* moles of solute} = .383 \frac{\text{mole}}{\text{kg}} \times 400 \text{ kg} = 0.153 \text{ mole}$$

$$\textcircled{3} \quad \text{molar mass} = \frac{12.6 \text{ g}}{0.153 \text{ mole}} = \begin{matrix} 82 \\ \uparrow \\ \text{Two} \\ \text{Sig fig} \end{matrix} \frac{\text{g}}{\text{mole}}$$

2) Chloroform and methanol form an ideal solution. The solution boils at 22 °C and 0.255 atm. At 22 °C, the vapor pressure of pure methanol is 0.192 atm and the vapor pressure of pure chloroform is 0.311 atm.

$$P_{\text{total}} = X_{\text{methanol}} P_{\text{methanol}} + X_{\text{chloroform}} P_{\text{chloroform}}$$

$$0.255 \text{ atm} = X_{\text{methanol}} (0.192 \text{ atm}) + (1 - X_{\text{methanol}}) 0.311 \text{ atm}$$

$$.255 = 0.192 X_{\text{methanol}} + .311 - .311 X_{\text{methanol}}$$

$$0.311 X_{\text{methanol}} - 0.192 X_{\text{methanol}} = 0.311 - .255$$

$$0.119 X_{\text{methanol}} = 0.056$$

$$X_{\text{methanol}} = \frac{.056}{.119} = 0.476$$

$$X_{\text{chloroform}} = 1 - 0.476 \\ = 0.524$$

3) What is the normal boiling point of 1.21 M solution of  $\text{CaI}_2$  that has a density of 1.92 g/ml? (  $K_B$  for  $\text{H}_2\text{O}$  =  $0.512^\circ \text{C} \cdot \text{kg/mole}$ )

Answer:  $101.2^\circ \text{C}$

① Find molality:

$1.21 \text{ mole } \text{CaI}_2 \xrightarrow{\text{in}} 1 \text{ liter}$

a) mass of solution :  $1000 \text{ ml solution} \left( \frac{1.92 \text{ g solution}}{1 \text{ ml solution}} \right) = 1920 \text{ g solution}$

b) mass of solute :

$$1.21 \text{ mole } \text{CaI}_2 \left( \frac{294 \text{ g } \text{CaI}_2}{1 \text{ mole } \text{CaI}_2} \right) = 356 \text{ g } \text{CaI}_2$$

c) mass of  $\text{H}_2\text{O}$  in  $1920 \text{ g solution} - 356 \text{ g } \text{CaI}_2 = 1564 \text{ g } \text{H}_2\text{O}$

d) molality :  $\frac{1.21 \text{ mole } \text{CaI}_2}{1.564 \text{ kg } \text{H}_2\text{O}} = 0.774 \frac{\text{mole}}{\text{kg}}$

$$\Delta T_{B.P} = i K_B \text{ molality} \\ = 3 \left( 0.512 \frac{^\circ \text{C}}{\text{mole}} \cdot \text{kg} \right) \cdot 0.774 \frac{\text{mole}}{\text{kg}} = 1.2^\circ \text{C}$$

$$B.P = 100 + 1.2 = 101.2^\circ \text{C}$$

4) Calculate the freezing point of a 36.0 % by mass  $\text{Na}_3\text{PO}_4$  solution. ( $K_f$  for  $\text{H}_2\text{O} = 1.86^\circ \text{C} \cdot \text{kg/mole}$ )

Answer:  $-25.5^\circ \text{C}$

$$36.0 \text{ g } \text{Na}_3\text{PO}_4 \xrightarrow{\text{in}} 64.0 \text{ g } \text{H}_2\text{O}$$

e)  $36.0 \text{ g } \text{Na}_3\text{PO}_4 \left( \frac{1 \text{ mole } \text{Na}_3\text{PO}_4}{164 \text{ g } \text{Na}_3\text{PO}_4} \right) = 0.220 \text{ mole } \text{Na}_3\text{PO}_4$

f) molality =  $\frac{0.220 \text{ mole } \text{Na}_3\text{PO}_4}{0.0640 \text{ kg solvent}} = 3.43 \frac{\text{mole}}{\text{kg}}$

$$\Delta T_{f.p} = i K_f \text{ molality}$$

$$= 4 \left( 1.86 \frac{^\circ \text{C} \cdot \text{kg}}{\text{mole}} \right) 3.43 \frac{\text{mole}}{\text{kg}}$$

$$= 25.5^\circ \text{C}$$

$$T_{f.p} = 0 - 25.5^\circ \text{C} = -25.5^\circ \text{C}$$

5) 32.00 ml of 0.311 M aluminum nitrate is mixed with 64.00 ml of 0.177 M sodium carbonate and allowed to react.

a) Write a balanced equation for the reaction.  $2 \text{Al}(\text{NO}_3)_3(\text{aq}) + 3 \text{Na}_2\text{CO}_3(\text{aq}) \rightarrow \text{Al}_2(\text{O}_3)_3(\text{s}) + 6 \text{NaNO}_3(\text{aq})$

Total-ionic:

Net-ionic:

c) Give the name and mass of any precipitate that may have formed.

Answer: 0.884 g of  $\text{Al}_2(\text{CO}_3)_3$  precipitate

d) Calculate the molar concentration of each ion remaining in solution after reaction is complete.

Answer: Concentration of carbonate ions = 0 M

Concentration of aluminum ions = 0.0252 M

Concentration of nitrate ions = 0.312 M

Concentration of sodium ions = 0.236 M

i) moles of  $\text{Al}(\text{NO}_3)_3$  available:

$$\text{M}_{\text{Al}(\text{NO}_3)_3} V_{\text{Al}(\text{NO}_3)_3} = \frac{0.311 \text{ mole}}{\text{L}} \times 0.03200 \text{ L}$$
$$= 9.95 \times 10^{-3} \text{ mole Al}(\text{NO}_3)_3$$

ii) moles of  $\text{Na}_2\text{CO}_3$  available:

$$\text{M}_{\text{Na}_2\text{CO}_3} V_{\text{Na}_2\text{CO}_3} = \frac{0.177 \text{ mole}}{\text{L}} \times 0.06400 \text{ L}$$
$$= 0.01133 \text{ mole Na}_2\text{CO}_3$$

iii) find limiting reagent:  
theoretical ratio of moles

$$\frac{\text{mole Na}_2\text{CO}_3}{\text{mole Al}(\text{NO}_3)_3} = \frac{3}{2} = \frac{1.5}{1}$$

Available ratio of moles:  
 $\frac{\text{mole Na}_2\text{CO}_3}{\text{mole Al}(\text{NO}_3)_3} = \frac{0.01133 \text{ mole}}{0.00995 \text{ mole}} = \frac{1.14}{1}$

$\text{Na}_2\text{CO}_3$  is the limiting reagent.

$$0.01133 \text{ mole Na}_2\text{CO}_3 \left( \frac{1 \text{ mole Al}_2(\text{O}_3)_3}{3 \text{ moles Na}_2\text{CO}_3} \right) \left( \frac{234 \text{ g Al}_2(\text{O}_3)_3}{1 \text{ mole Al}_2(\text{O}_3)_3} \right) = 0.884 \text{ g Al}_2(\text{O}_3)_3$$

precipitate

Find moles of excess reagent,  $\text{Al}(\text{NO}_3)_3$  left over:

$$0.01133 \text{ mole Na}_2\text{CO}_3 \left( \frac{2 \text{ moles Al}(\text{NO}_3)_3}{3 \text{ moles Na}_2\text{CO}_3} \right) = 0.00753 \text{ mole Al}(\text{NO}_3)_3$$

$$\text{moles of Al}(\text{NO}_3)_3 \text{ left over} = 9.95 \times 10^{-3} \text{ mole} - 7.53 \times 10^{-3} \text{ mole}$$
$$= 2.42 \times 10^{-3} \text{ mole Al}(\text{NO}_3)_3$$

left over

Find moles  $\text{NaNO}_3$  formed:

$$0.01133 \text{ mole Na}_2\text{CO}_3 \left( \frac{6 \text{ moles NaNO}_3}{3 \text{ moles Na}_2\text{CO}_3} \right) = 0.0227 \text{ mole NaNO}_3 \text{ formed}$$

Find concentration of ions in solution:

a) moles of  $\text{Al}^{3+}$  from  $\text{Al}(\text{NO}_3)_3$  left over:-

$$0.00242 \text{ mole Al}(\text{NO}_3)_3 \left( \frac{1 \text{ mole Al}^{3+}}{1 \text{ mole Al}(\text{NO}_3)_3} \right) = 0.00242 \text{ mole Al}^{3+}$$

$$[\text{Al}^{3+}] = \frac{0.00242 \text{ mole}}{0.0960 \text{ L}} = 0.0252 \text{ M}$$

$$[\text{NO}_3^-] = \frac{(0.00242 \times 3) \text{ mole}}{0.0960 \text{ L}} = 0.312 \text{ M}$$

$$[\text{O}_3^{2-}] = 0 \text{ M}$$

**SET C:**

1) What is the molarity of an aqueous solution of  $C_6H_{12}O_6$  that has a normal boiling point of  $101.40^\circ C$  and density of  $1.68 \text{ g/ml}$ ?  $K_B$  for water is  $0.512^\circ C \cdot \text{kg}/\text{mole}$ . ( $C_6H_{12}O_6$  is a nonvolatile nondissociating solute.)

$$\textcircled{1} \quad \Delta T_B = K_B \text{ molality}$$

Answer:  $3.07 \text{ mole/L}$

$$1.40^\circ C = 0.512^\circ C \cdot \text{kg} \cdot \text{molality}$$

$$\text{molality} = \frac{\text{mole } C_6H_{12}O_6}{\frac{140^\circ C}{0.512 \text{ kg}} \cdot \text{mole}} = 2.73 \frac{\text{mole solute}}{\text{kg } H_2O}$$

$$\textcircled{2} \quad \text{Change } 2.73 \text{ mole } C_6H_{12}O_6 \text{ into mass:}$$

$$2.73 \text{ mole } C_6H_{12}O_6 \left( \frac{180.0 \text{ g } C_6H_{12}O_6}{1 \text{ mole } C_6H_{12}O_6} \right) = 491 \text{ g } C_6H_{12}O_6$$

$$\textcircled{3} \quad \text{Find mass of solution:}$$

$$491 \text{ g } C_6H_{12}O_6 + 1000 \text{ g } H_2O = 1491 \text{ g solution}$$

$$\textcircled{4} \quad \text{Find volume of solution:}$$

$$1491 \text{ g solution} \left( \frac{1 \text{ ml solution}}{1.68 \text{ g solution}} \right) = 888 \text{ ml solution}$$

$$\textcircled{5} \quad \text{Molarity} = \frac{\text{no of moles of solute}}{\text{Liters of solution}}$$

$$= \frac{2.73 \text{ mole } C_6H_{12}O_6}{0.888 \text{ L}} = \underline{\underline{3.07 \frac{\text{mole}}{\text{L}}}}$$

2) Calculate the normal freezing point of a  $0.6837 \text{ M}$  aqueous solution of  $C_{12}H_{22}O_{11}$  that has a density of  $1.35 \text{ g/ml}$ . ( $C_{12}H_{22}O_{11}$  is a nonvolatile nondissociating solute.) The molal freezing point depression constant of water is  $1.86^\circ C \cdot \text{kg}/\text{mole}$ .

Answer: Freezing point =  $-1.14^\circ C$

$$\textcircled{1} \quad \text{Change } 0.6837 \text{ mole } C_{12}H_{22}O_{11} \text{ into mass } C_{12}H_{22}O_{11}:$$

$$0.6837 \text{ mole } C_{12}H_{22}O_{11} \left( \frac{342.2 \text{ g } C_{12}H_{22}O_{11}}{1 \text{ mole } C_{12}H_{22}O_{11}} \right) = 234.0 \text{ g } C_{12}H_{22}O_{11}$$

$$\textcircled{2} \quad \text{mass of solution:}$$

$$1000 \text{ ml solution} \left( \frac{1.35 \text{ g solution}}{1 \text{ ml solution}} \right) = 1350 \text{ g solution}$$

$$\textcircled{3} \quad \text{mass of } H_2O: 1350 \text{ g solution} - 234.0 \text{ g solute} = 1116 \text{ g } H_2O$$

$$\textcircled{4} \quad \text{molality} = \frac{\text{moles of solute}}{\text{kg of } H_2O} = \frac{0.6837 \text{ mole solute}}{1.116 \text{ kg } H_2O} = 0.6126 \frac{\text{mole}}{\text{kg}}$$

$$\textcircled{5} \quad \Delta T_f = K_f \text{ molality}$$

$$= 1.86 \frac{\circ C \cdot \text{kg}}{\text{mole}} (0.6126 \frac{\text{mole}}{\text{kg}})$$

$$= 1.14^\circ C$$

$$\textcircled{6} \quad \text{freezing point} = -1.14^\circ C$$

3) Heptane, C<sub>7</sub>H<sub>16</sub>, and octane, C<sub>8</sub>H<sub>18</sub>, form ideal solutions. At 40. °C, the vapor pressure of pure heptane is 0.522 atm, and the vapor pressure of pure octane is 0.238 atm. A solution is made of 5.32 g heptane and 8.80 g octane. Calculate the mole fraction of octane in the vapor at the above temperature.

Answer: 0.398

$$\begin{aligned}
 \text{Total vapor pressure} &= X_{\text{heptane}} P^{\circ}_{\text{heptane}} + X_{\text{octane}} P^{\circ}_{\text{octane}} \\
 &= \frac{\frac{5.32\text{g}}{100.1\text{g/mole}}}{\frac{5.32\text{g}}{100.1\text{g/mole}} + \frac{8.80\text{g}}{114.2\text{g/mole}}} (.522\text{atm}) + \frac{\frac{8.80\text{g}}{114.2\text{g/mole}}}{\frac{5.32\text{g}}{100.1\text{g/mole}} + \frac{8.80\text{g}}{114.2\text{g/mole}}} (.238\text{atm}) \\
 &= \frac{0.0531\text{ mole}}{(0.0531 + 0.0771)\text{ mole}} (.522\text{atm}) + \frac{0.0771}{(0.0531 + 0.0771)\text{ mole}} (.238\text{atm}) \\
 &= \frac{0.0531}{0.130} (.522\text{atm}) + \frac{0.0771}{0.130} (.238\text{atm}) \\
 &= (0.408) (.522\text{atm}) + .593 (.238) \\
 &= .213\text{ atm} + 0.141\text{ atm} = 0.354\text{ atm} \\
 X_{\text{octane}} \text{ in vapor} &= X_{\text{octane}} \text{ Total} ; 0.141\text{atm} = X_{\text{octane}} \text{ in vapor} (.354\text{ atm}) \\
 X_{\text{octane}} \text{ in vapor} &= \frac{0.141}{0.354} = \underline{\underline{0.398}}
 \end{aligned}$$

4) What is the molar mass and molecular formula of a nondissociating compound whose empirical formula is C<sub>4</sub>H<sub>2</sub>N, if 3.84 g of the compound in 500. g benzene give a freezing point depression of 0.307 °C? (The molal freezing point depression constant for benzene is 5.12 °C · kg/mole.)

Answer: 128 g/mole; C<sub>8</sub>H<sub>4</sub>N<sub>2</sub>

$$\textcircled{1} \quad \Delta T = K_f \text{ molality}$$

$$0.307\text{ }^{\circ}\text{C} = 5.12 \frac{\text{ }^{\circ}\text{C} \cdot \text{kg}}{\text{mole}} \text{ molality}$$

$$\text{molality} = 0.0600 \frac{\text{mole}}{\text{kg}}$$

$$\textcircled{2} \quad \text{molality} = \frac{\text{* moles of solute}}{\text{kg of solvent}}$$

$$\text{* moles of solute: } \frac{0.600\text{ mole}}{\text{kg}} \times \frac{.500\text{ kg solvent}}{\text{solute}} = .0300 \frac{\text{mole}}{\text{solute}}$$

$$\textcircled{3} \quad \text{molar mass: } \frac{3.84\text{ g solute}}{.0300\text{ mole solute}} = 128 \frac{\text{g}}{\text{mole}}$$

$$\textcircled{4} \quad \text{molar mass of empirical formula, C}_4\text{H}_2\text{N} = 64.0 \frac{\text{g}}{\text{mole}}$$

$$\frac{\text{mass of molecular formula}}{\text{mass of empirical formula}} = \frac{128\text{ g/mole}}{64.0\text{ g/mole}} = \frac{2}{1}$$

5) Liquids A and B form an ideal solution. The vapor pressure of pure A is 0.700 atm at the normal boiling point of a solution prepared from 0.250 mole of B and 0.650 mole of A. What is the vapor pressure of pure B at this temperature?

$$\begin{aligned} P_{\text{total}} &= P_A + P_B \\ &= X_A P_A^{\circ} + X_B P_B^{\circ} \\ 1 \text{ atm} &= \frac{.650}{.250+.650} (.700 \text{ atm}) + \frac{.250}{(.250+.650)} P_B^{\circ} \\ 1 \text{ atm} &= .722 (.700 \text{ atm}) + .278 P_B^{\circ} \\ 1 \text{ atm} &= .506 + .278 P_B^{\circ} \\ 1.00 - .506 &= .278 P_B^{\circ} \\ .494 &= .278 P_B^{\circ} \\ P_B^{\circ} &= \frac{.494}{.278} = 1.77 \text{ atm} \end{aligned}$$

6) A 0.900 L aqueous solution contains 30.0 g of a protein. The osmotic pressure of the solution is 12.7 torr at 25 °C. What is the molar mass of the protein?

Answer:  $4.88 \times 10^4 \text{ g/mole}$

$$\textcircled{1} \quad \Pi = M R T$$

$$12.7 \text{ torr} \left( \frac{1 \text{ atm}}{760 \text{ torr}} \right) = M \left( 0.0821 \frac{\text{Latm}}{\text{moleK}} \right) 298 \text{ K}$$

$$M = 6.83 \times 10^{-4} \frac{\text{mole}}{\text{l}}$$

$$\textcircled{2} \quad \text{no of moles of protein} = M \times V$$

$$= 6.83 \times 10^{-4} \frac{\text{mole}}{\text{l}} \times 0.900 \text{ l}$$

$$= 6.15 \times 10^{-4} \text{ mole}$$

$$\textcircled{3} \quad \text{molar mass} = \frac{30.0 \text{ g protein}}{6.15 \times 10^{-4} \text{ mole protein}} = 4.88 \times 10^4 \text{ g/mole}$$

7) Acetone and methanol form ideal solution. At 25 °C, the vapor pressures of pure acetone and pure methanol are 0.342 atm and 0.188 atm respectively. Calculate the mole fraction of methanol in a solution that boils at 25 °C and 0.248 atm.

Answer:  $X = 0.610$

$$X_{\text{methanol}} + X_{\text{acetone}} = 1$$
$$P_{\text{total}} = X_{\text{acetone}} P^{\circ}_{\text{acetone}} + X_{\text{methanol}} P^{\circ}_{\text{methanol}}$$

$$= (1 - X_{\text{methanol}}) (0.342 \text{ atm}) + X_{\text{methanol}} (0.188)$$

$$0.248 \text{ atm} = (1 - X_{\text{methanol}}) 0.342 + X_{\text{methanol}} (0.188)$$

$$X_{\text{methanol}} = 0.610$$